ELECTRIC VEHICLE TECHNOLOGY EXPLAINED

ELECTRIC VEHICLE TECHNOLOGY EXPLAINED SECOND EDITION

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About the Author

John Lowry is a professional engineer who graduated in Mechanical Engineering from Imperial College, London University. He holds a PhD from Queen Mary College, London University. He was formerly a university lecturer and is currently a consultant engineer. He is a Fellow of the Institution of Mechanical Engineers, the Institute of Energy and the Institute of Engineering and Technology.

Preface

Electric vehicle technology is now in its third century of development and is likely to advance rapidly in the coming years.

Electric trains are widely used and modern high-speed trains are competitive with air travel in terms of journey speed over shorter land routes. In energy terms they use less than 10% of the fuel per passenger kilometre than air transport.

Electric road vehicles have not achieved the commercial success that internal combustion engine vehicles have; however, battery technology has now developed to the point where electric vehicles are being commercially produced. Future battery developments are likely to accelerate the use of electric road vehicles in the next few years.

Small electric vehicles such as golf buggies and personnel carriers in airports have become well established. Electric bicycles are becoming increasingly popular and are considered one of the fastest ways to move about crowded cities.

Potential environmental benefits which can result from the use of electric vehicles are substantial when the vehicles use electricity that is generated from sources which use highly efficient modern generating stations or which use nuclear or sustainable energy. Environmental benefits include zero exhaust emissions in the vicinity of the vehicles, reduced dependence on fossil fuels and reduced overall carbon emissions.

This book explains both the technology of electric vehicles and how they affect the environment. The book is designed for engineers and scientists who require a thorough understanding of electric vehicle technology and its effects on the environment.

John Lowry

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Abbreviations

Anti-lock brake system
Alternating current
Alkaline fuel cell
Brushless DC (motor)
Balance of plant
Computer-aided design
Computer-aided manufacturing
California Air Resources Board
Combined cycle gas turbine
Computational fluid dynamics
Combined heat and power
Central Japan Railway
Compressed natural gas
Catalytic partial oxidation
Direct current
Direct methanol fuel cell
Degree of hybridisation
Double overhead cam
Electronically controlled continuous variable transmission
Electronically commutated motor
Electric Fuel Transportation Company
Electromotive force
Environmental Protection Agency
Electric power steering
Energy Technology Support Unit (a UK government organisation)
Extra-Urban Driving Cycle
Electric vehicle
Fuel cell
Fuel cell vehicle
Federal Highway Driving Schedule
Federal Urban Driving Schedule
General Motors
General Motors Electric Vehicle 1

GNF	Graphitic nanofibre
GRP	Glass reinforced plastic
GTO	Gate turn-off
HEV	Hybrid electric vehicle
HHV	Higher heating value
HSR	High-speed rail
HSST	High-speed surface train
IC	Internal combustion
ICE	Internal combustion engine
IEC	International Electrotechnical Commission
IGBT	Insulated gate bipolar transistor
IMA	Integrated Motor Assist
IPT	Inductive power transfer
JET	Joint Euorpean Torus
kph	Kilometres per hour
LH ₂	Liquid (cryogenic) hydrogen
LHV	Lower heating value
LIB	Lithium ion battery
LPG	Liquid petroleum gas
LSV	Low-speed vehicle
MCFC	Molten carbonate fuel cell
MeOH	Methanol
MEA	Membrane electrode assembly
MOSFET	Metal oxide semiconductor field effect transistor
mph	Miles per hour
NASA	National Aeronautics and Space Administration
NEDC	New European Driving Cycle
NiCad	Nickel cadmium (battery)
NiMH	Nickel metal hydride (battery)
NL	Normal litre, 1 litre at NTP
NOx	Nitrous oxides
NTP	Normal temperature and pressure (20 °C and 1 atm or 1.013 25 bar)
OCV	Open-circuit voltage
PAFC	Phosphoric acid fuel cell
PEM	Proton exchange membrane OR polymer electrolyte membrane (different names for the same thing which fortunately have the same abbreviation)
PEMFC	Proton exchange membrane fuel cell OR polymer electrolyte membrane fuel cell
PM	Permanent magnet OR particulate matter
POX	Partial oxidation
ppb	Parts per billion
ppm	Parts per million
PROX	Preferential oxidation
PSA	Pressure swing absorption

PTFE	Polytetrafluoroethylene
PZEV	Partial zero-emission vehicle
RRIM	Reinforced reaction injection moulding
SAE	Society of Automotive Engineers
SFUDS	Simplified Federal Urban Driving Schedule
SL	Standard litre, 1 litre at STP
SLI	Starting, lighting and ignition
SMC	Sheet moulding compound
SOC	State of charge
SOFC	Solid oxide fuel cell
SRM	Switched reluctance motor
STP	Standard temperature and pressure
SULEV	Super ultra-low-emission vehicle
SUV	Sports utility vehicle
TDI	Toyota Direct Ignition
TGV	Train à grande vitesse
VOC	Volatile organic compound
VRLA	Valve-regulated (sealed) lead acid (battery)
WOT	Wide open throttle
ZEBRA	Zero Emissions Battery Research Association
ZEV	Zero-emission vehicle

Symbols

Letters are used to stand for variables, such as mass, and also as chemical symbols in chemical equations. The distinction is usually clear from the context, but for even greater clarity italics are used for variables and ordinary text for chemical symbols, so H stands for enthalpy, whereas H stands for hydrogen.

In cases where a letter can stand for two or more variables, the context always makes it clear which is intended.

a	Acceleration
Α	Area
В	Magnetic field strength
С	Amphour capacity of a battery OR capacitance of a capacitor
<i>C</i> ₃	Amphour capacity of a battery if discharged in 3 hours, the '3 hour rate'
C_d	Drag coefficient
C_p	Peukert capacity of a battery, the same as the amphour capacity if discharged at a current of 1 amp
CR	Charge removed from a battery, usually in amphours
CS	Charge supplied to a battery, usually in amphours
d	Separation of the plates of a capacitor, OR distance travelled
DoD	Depth of discharge, a ratio changing from 0 (fully charged) to 1 (empty)
е	Magnitude of the charge on one electron, 1.602×10^{-19} coulombs
Ε	Energy OR Young's modulus OR EMF (voltage)
E_{b}	Back EMF (voltage) of an electric motor in motion
E_{f}	Field winding
$\vec{E_s}$	Supplied EMF (voltage) to an electric motor
f	Frequency
F	Force OR Faraday constant, the charge on 1 mole of electrons, 96 485 coulombs
F_{ad}	Force needed to overcome the wind resistance on a vehicle
F_{la}	Force needed to give linear acceleration to a vehicle
F_{hc}	Force needed to overcome the gravitational force of a vehicle down a hill
F _{rr}	Force needed to overcome the rolling resistance of a vehicle
F _{te}	Tractive effort, the forward driving force on the wheels

$F_{\omega a}$	Force at the wheel needed to give rotational acceleration to the rotating parts of a vehicle
g	Acceleration due to gravity
G	Gear ratio OR rigidity modulus OR Gibbs free energy (negative thermodynamic potential)
Н	Enthalpy
Ι	Current OR moment of inertia OR second moment of area (the context makes it clear)
I	Motor current
I m	Polar second moment of area
k	Peukert coefficient
k.	Copper losses coefficient for an electric motor
k.	Iron losses coefficient for an electric motor
k_{\dots}	Windage losses coefficient for an electric motor
KĔ	Kinetic energy
<i>K</i>	Motor constant
L^{m}	Length
т	Mass
'n	Mass flowrate
m_{h}	Mass of batteries
n	Number of cells in a battery OR a fuel cell stack OR the number of moles of substance
Ν	Avogadro's number, 6.022×10^{23} , OR revolutions per second
Р	Power OR pressure
P _{adb}	Power from the battery needed to overcome the wind resistance on a vehicle
P_{adw}	Power at the wheels needed to overcome the wind resistance on a vehicle
P_{hc}^{aan}	Power needed to overcome the gravitational force of a vehicle down a hill
P _{mot-in}	Electrical power supplied to an electric motor
P _{mot-out}	Mechanical power given out by an electric motor
P_{rr}	Power needed to overcome the rolling resistance of a vehicle
P_{te}	Power supplied at the wheels of a vehicle
q	Sheer stress
Q	Charge (e.g. in a capacitor)
r	Radius, of wheel, axle, OR the rotor of a motor, etc.
R	Electrical resistance OR the molar gas constant $8.314 \mathrm{J}\mathrm{K}^{-1}\mathrm{mol}^{-1}$
r_i, r_o	Inner and outer radius of a hollow tube
R_a	Armature resistance of a motor or generator
R_L	Resistance of a load
S	Entropy
SE	Specific energy
Т	Temperature OR Torque OR the discharge time of a battery in hours
T_1, T_2	Temperatures at different stages in a process
T_{f}	Frictional torque (e.g. in an electric motor)
t_{ON}, t_{OFF}	On and off times for a chopper circuit
v	Velocity

V	Voltage
W	Work done
z	Number of electrons transferred in a reaction
δ	Deflection
δt	Time step in an iterative process
Δ	Change in, e.g. ΔH = change in enthalpy
ε	Electrical permittivity
η	Efficiency
η_c	Efficiency of a DC/DC converter
η_{fc}	Efficiency of a fuel cell
η_g	Efficiency of a gearbox
η_m	Efficiency of an electric motor
η_o	Overall efficiency of a drive system
θ	Angle of deflection or bend
λ	Stoichiometric ratio
μ_{rr}	Coefficient of rolling resistance
ρ	Density
σ	Bending stress
Φ	Total magnetic flux
ψ	Angle of slope or hill
ω	Angular velocity