## Appendix H

# Worked Example for the Calculation of Earthing Current and Electric Shock Hazard Potential Difference in a Rod and Grid Earthing System 

## H. 1 WORKED EXAMPLE

A 33 kV overhead line terminates at a pole in a small switching station. The distance to the pole from the source is 15 km , but of course there are many other poles along the route. The subject pole is earthed at its footings.

The overhead line ohmic data are:-
Positive sequence impedance $Z_{1 \mathrm{pkm}}=0.35+j 0.4 \mathrm{ohms} / \mathrm{km}$.
Negative sequence impedance $Z_{2 \mathrm{pkm}}=0.35+j 0.4 \mathrm{ohms} / \mathrm{km}$.
Zero sequence impedance $Z_{0 \mathrm{pkm}}=0.7+j 1.5 \mathrm{ohms} / \mathrm{km}$.
The sending end of the line has a 100 MVA transformer that has the following ohmic data:-
Positive sequence impedance $Z_{1 t}=0.1084+j 1.084 \mathrm{ohms} / \mathrm{phase}$.
Negative sequence impedance $Z_{2 t}=Z_{1 t}$ ohms/phase.
Zero sequence impedance $Z_{0 t}=Z_{1 t}$ ohms/phase.

It will be assumed that the source impedance $Z_{s}$ feeding the transformers is small enough to be neglected. To illustrate the difficulty in finding a suitably low resistance to earth it will be assumed that the secondary winding of the transformer is solidly earthed and hence the NER resistance $R_{n}$ is zero, a non-zero value will be recommended at the conclusion of the calculations. However, it will be assumed that the resistance to earth $R_{\text {en }}$ at the source transformer is 1.5 ohms . The resistance to earth at the far end pole is $R_{\text {ep }}$, which needs to be determined. This requires a suitable grid and rod system to be chosen. The calculation process will be carried out in a series of steps.

Step 1. Find the total positive, negative and zero sequence impedances in the circuit.
The total positive sequence impedance $Z_{1}$ is:-

$$
\begin{aligned}
Z_{1} & =15.0(0.35+j 0.4)+0.1084+j 1.084 \\
& =5.3584+j 7.084 \mathrm{ohms}
\end{aligned}
$$

The total negative sequence impedance $Z_{2}$ is:-

$$
Z_{2}=Z_{1}=5.3584+j 7.084 \mathrm{ohms}
$$

The total zero sequence impedance $Z_{0}$ is:-

$$
\begin{align*}
Z_{0} & =\frac{15.0 Z_{0 \mathrm{pkm}}\left(R_{\mathrm{en}}+R_{\mathrm{ep}}\right)}{\left(15.0 \times Z_{0 \mathrm{pkm}}\right)+R_{\mathrm{en}}+R_{\mathrm{ep}}}+Z_{0 p}+Z_{0 t} \\
& =\frac{(10.5+j 22.5)\left(1.5+R_{\mathrm{ep}}\right)}{12.0+R_{\mathrm{ep}}+j 22.5}+10.6084+j 23.584 \tag{H.1.1}
\end{align*}
$$

Hence $Z_{0}$ is a function of $R_{\mathrm{ep}}$.
In this worked example the zero sequence impedance includes the impedance of the over-head earthing conductor as a simple conductor spanning the 15 km route length. In practice the intermediate poles will be earthed at their own footings and also bonded to the over-head earthing conductor. These bonding connections will form a type of 'ladder' network that involves the resistance to earth at each pole. The effect of this may be to reduce the amount of current entering the ground at the far end pole, i.e. the subject of these calculations. Table H.1a would then contain different values of currents.

Step 2. Find the total root-mean-square fault current.
The total root-mean-square fault current $I_{f}$ is:-

$$
\begin{equation*}
I_{f}=3 I_{0}=\frac{3 V_{p}}{3 R_{f}+Z_{1}+Z_{2}+Z_{0}} \tag{H.1.2}
\end{equation*}
$$

Where $I_{0}=$ the symmetrical rms zero sequence current.
$V_{p}=$ the phase-to-neutral driving voltage at the source.
$R_{f}=$ the resistance of the fault itself, assumed to be zero.
$Z_{1}=$ the total positive sequence impedance.
$Z_{2}=$ the total negative sequence impedance.
$Z_{0}=$ the total zero sequence impedance.

Therefore inserting the numerical data gives,

$$
\begin{aligned}
& R_{1}=5.3584 \text { ohms }, \quad X_{1}=7.084 \text { ohms } \\
& R_{2}=5.3584 \text { ohms }, \quad X_{2}=7.084 \text { ohms }, \\
& R_{0}=\text { real part of } Z_{0}, \quad X_{0}=\text { imaginary part of } Z_{0} . \\
& V_{p}=33,000 / \sqrt{ } 3=19,053 \text { volts } / \text { phase } .
\end{aligned}
$$

Table H.1a. Earth fault current as a function of earth resistance

| Earth resistance (ohms) | Earth fault current (amps) | Proportion of current diverted to the |  | $\begin{gathered} \text { X-to-R } \\ \text { ratio } \\ \text { (pu) } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: |
|  |  | $\mathrm{O} / \mathrm{H}$ line (pu) | Pole <br> (pu) |  |
| 0.25 | 1314.73 | 0.0683 | 0.9692 | 1.6023 |
| 0.50 | 1310.23 | 0.0777 | 0.9647 | 1.5876 |
| 0.75 | 1305.70 | 0.0870 | 0.9601 | 1.5736 |
| 1.00 | 1301.13 | 0.0962 | 0.9555 | 1.5602 |
| 1.25 | 1296.54 | 0.1053 | 0.9509 | 1.5474 |
| 1.50 | 1201.92 | 0.1143 | 0.9463 | 1.5351 |
| 1.75 | 1287.30 | 0.1233 | 0.9416 | 1.5233 |
| 2.00 | 1282.66 | 0.1321 | 0.9370 | 1.5121 |
| 4.00 | 1245.83 | 0.1992 | 0.8993 | 1.4383 |
| 6.00 | 1210.65 | 0.2603 | 0.8617 | 1.3874 |
| 8.00 | 1178.15 | 0.3156 | 0.8248 | 1.3532 |
| 10.0 | 1148.73 | 0.3654 | 0.7890 | 1.3311 |
| 15.0 | 1088.41 | 0.4695 | 0.7065 | 1.3094 |
| 20.0 | 1043.88 | 0.5496 | 0.6347 | 1.3141 |
| 25.0 | 1010.86 | 0.6120 | 0.5734 | 1.3307 |
| 30.0 | 985.98 | 0.6611 | 0.5211 | 1.3523 |
| 35.0 | 966.84 | 0.7005 | 0.4754 | 1.3754 |
| 40.0 | 951.83 | 0.7325 | 0.4382 | 1.3985 |
| 50.0 | 930.11 | 0.7808 | 0.3765 | 1.4417 |
| 60.0 | 915.38 | 0.8153 | 0.3292 | 1.4794 |
| 70.0 | 904.88 | 0.8409 | 0.2920 | 1.5120 |
| 80.0 | 897.07 | 0.8605 | 0.2622 | 1.5399 |
| 90.0 | 891.08 | 0.8760 | 0.2377 | 1.5640 |
| 100.0 | 886.36 | 0.8885 | 0.2173 | 1.5850 |

Note 1. These are in relation to the magnitude of the total current, since both currents are complex quantities having different phase angles.

Table H.1a shows the value of $I_{f}$ for different values of $R_{\text {ep }}$. It also shows the division of current between the overhead line earthing conductor and the footings of the pole.

Table H.1b shows the 'doubling factor', the peak factor and the power factor of currents that flow in an inductive circuit that has different X-to-R or R-to-X factors.

A small site may be constrained by a number of factors. Assume the site is located in a region of high resistivity with a low water table. The constraints on the design are:-

- The surface resistivity is higher than that of the lower soil.
- A grid with earthing rods attached will be needed.
- Use a rod diameter no less than 0.01 m .
- Allow the rods to be driven deep into the ground.
- Use the least site area as possible, i.e. 30 to $256 \mathrm{~m}^{2}$.
- Let the overhead earthing conductor divert some of the fault current.

Table H.1b. Properties of the fault current for different X-to-R ratios

| X-to-R <br> ratio <br> (pu) | $\begin{gathered} \text { R-to-X } \\ \text { ratio } \\ \text { (pu) } \end{gathered}$ | Doubling factor (pu) | Peak <br> factor <br> (pu) | Power factor (pu) |
| :---: | :---: | :---: | :---: | :---: |
| 0.1 | 10.0000 | 1.0000 | 1.4142 | 0.9950 |
| 0.2 | 5.0000 | 1.0000 | 1.4142 | 0.9806 |
| 0.3 | 3.3333 | 1.0000 | 1.4143 | 0.9578 |
| 0.4 | 2.5000 | 1.0004 | 1.4148 | 0.9285 |
| 0.5 | 2.0000 | 1.0019 | 1.4169 | 0.8944 |
| 0.6 | 1.6667 | 1.0053 | 1.4217 | 0.8575 |
| 0.7 | 1.4286 | 1.0112 | 1.4301 | 0.8192 |
| 0.8 | 1.2500 | 1.0197 | 1.4421 | 0.7809 |
| 0.9 | 1.1111 | 1.0305 | 1.4573 | 0.7433 |
| 1.0 | 1.0000 | 1.0432 | 1.4753 | 0.7071 |
| 1.1 | 0.9091 | 1.0575 | 1.4955 | 0.6727 |
| 1.2 | 0.8333 | 1.0729 | 1.5174 | 0.6402 |
| 1.3 | 0.7692 | 1.0892 | 1.5404 | 0.6097 |
| 1.4 | 0.7143 | 1.1060 | 1.5642 | 0.5812 |
| 1.5 | 0.6667 | 1.1231 | 1.5884 | 0.5547 |
| 1.6 | 0.6250 | 1.1404 | 1.6127 | 0.5300 |
| 1.7 | 0.5882 | 1.1576 | 1.6370 | 0.5070 |
| 1.8 | 0.5556 | 1.1746 | 1.6611 | 0.4856 |
| 1.9 | 0.5263 | 1.1914 | 1.6859 | 0.4657 |
| 2.0 | 0.5000 | 1.2079 | 1.7082 | 0.4472 |
| 3.0 | 0.3333 | 1.3509 | 1.9105 | 0.3162 |
| 4.0 | 0.2500 | 1.4559 | 2.0590 | 0.2425 |
| 5.0 | 0.2000 | 1.5335 | 2.1687 | 0.1961 |
| 6.0 | 0.1667 | 1.5924 | 2.2520 | 0.1644 |
| 7.0 | 0.1429 | 1.6384 | 2.3170 | 0.1414 |
| 8.0 | 0.1250 | 1.6752 | 2.3691 | 0.1240 |
| 9.0 | 0.1111 | 1.7053 | 2.4117 | 0.1104 |
| 10.0 | 0.1000 | 1.7304 | 2.4472 | 0.0995 |
| 15.0 | 0.0667 | 1.8110 | 2.5612 | 0.0665 |
| 20.0 | 0.0500 | 1.8546 | 2.6229 | 0.0499 |
| 25.0 | 0.0400 | 1.8819 | 2.6614 | 0.0400 |
| 30.0 | 0.0333 | 1.9006 | 2.6878 | 0.0333 |
| 35.0 | 0.0286 | 1.9142 | 2.7070 | 0.0286 |
| 40.0 | 0.0250 | 1.9245 | 2.7216 | 0.0250 |
| 45.0 | 0.0222 | 1.9326 | 2.7331 | 0.0222 |
| 50.0 | 0.0200 | 1.9391 | 2.7423 | 0.0200 |
| 100.0 | 0.0100 | 1.9691 | 2.7847 | 0.0100 |
| 200.0 | 0.0050 | 1.9844 | 2.8064 | 0.0050 |
| 300.0 | 0.0033 | 1.9896 | 2.8137 | 0.0033 |
| 400.0 | 0.0025 | 1.9922 | 2.8174 | 0.0025 |
| 500.0 | 0.0020 | 1.9937 | 2.8196 | 0.0020 |

- Use the method described in IEEE80 sub-section 14.4 even though it is more applicable to much larger sites, but include the earthing rods.
- If possible limit the maximum resistance to earth at the site to 5 ohms.

Step 3. Find the resistance $R_{\text {ep }}$ at the pole.
The following calculations are based on the methods given in IEEE80 Appendix C. The same symbols and notation are generally used to avoid confusion with the reference. The design data and constraints are:-

- Fault duration
- Resistivity of lower layer
- Resistivity of upper layer
- Thickness of upper layer
- Depth of burial of grid
- Site area
- Diameter of rods
- Depth of each rod
- Number of meshes in each side of the grid
- Spacing between the mesh nodes

$$
\begin{array}{ll}
t_{s} & =0.5 \mathrm{sec} \\
\rho & =100 \text { to } 1000 \text { ohm-m } \\
\rho_{s} & =1000 \text { to } 5000 \text { ohm-m } \\
h_{s} & =0.2 \text { and } 1.0 \mathrm{~m} \\
h & =0.5 \text { and } 1.0 \mathrm{~m} \\
A & =36 \text { to } 256 \mathrm{~m}^{2} \\
d_{r} & =0.02 \text { and } 0.2 \mathrm{~m} \\
l_{r} & =10 \text { and } 50 \mathrm{~m} \\
N_{\text {mesh }} & =3 \text { to } 8 \\
d_{\text {sp }} & =2.0 \mathrm{~m}
\end{array}
$$

The results of the calculations are shown in Table H.1c; Case C. 3 is used for the worked example. In this case the following additional information was used:-

- Number of outer peripheral rods
- Number of inner rods
- Number of rods on each side of grid
- Diameter of grid conductors

$$
\begin{aligned}
& N_{\text {rod1 }}=4 \\
& N_{\text {rod2 }}=0 \\
& N=2 \\
& d_{m}=0.01 \mathrm{~m}
\end{aligned}
$$

Calculate the resistivity derating factor $C_{s}\left\{h_{s}, K\right\}$ from (13.3), in which $u_{s}=\sqrt{ }(1+$ $\left(2 \mathrm{mh}_{s} / 0.08\right)^{2}$ ). The number of terms $m$ is taken to be 25 in order to obtain good convergence of the factor. The reflection factor $K$ is found from $\rho$ and $\rho_{s}$ to be -0.6667 per-unit. $C_{s}\left\{h_{s}, K\right\}$ is found to be 0.8338 for this example.

The approximate grid resistance $R_{\text {epo }}$ without the earthing rods can be found from Figure H.1a, which was derived from Figure B. 1 of IEEE80 but applicable to small sizes of the mesh $R_{\text {epo }}$, is approximately:-

$$
R_{\mathrm{epo}}=\frac{\rho 51.94}{1000}=51.94 \mathrm{ohms}
$$

which is too high and indicates the need for rods.
At this stage the 50 kg step and touch voltages can be calculated from $C_{s}\left\{h_{s}, K\right\}$, since $\rho_{s}$ and $t_{s}$ are constants. The step voltage $E_{\text {step50 }}$ is: -

$$
E_{\text {step50 }}=\frac{\left(1000+6 C_{s} \rho_{s}\right) 0.116}{\sqrt{ } t_{s}}=4267 \text { volts. }
$$



Figure H.1a Grid resistance versus the number of meshes on a side of a grid.

Similarly the touch voltage $E_{\text {touch50 }}$ is:-

$$
E_{\text {touch } 50}=\frac{\left(1000+1.5 C_{s} \rho_{s}\right) 0.116}{\sqrt{ } t_{s}}=1190 \text { volts. }
$$

These two equations apply as criteria whether or not earthing rods are used. At this stage the magnitude of the portion of the fault current $I_{f}$ entering the ground has not been used in the equations for voltages. It is necessary to calculate the corner mesh voltage $E_{m}$, which is given by equation 71 in IEEE80,

$$
E_{m}=\frac{\rho_{s} I_{g} K_{s} K_{i}}{L}=1854 \text { volts }
$$

after solving equations 68 and 69 for $K_{m}$ and $K_{i}$. However, $K_{m}$ is also dependent on the current flowing into the ground, $I_{\mathrm{fe}}$, and so the resistance to earth for the grid and rods must first be calculated. The corner mesh potential can also be found Figure H.1b, which was again derived from Figure B. 2 of IEEE80.

Calculate the constants $K_{1}$ and $K_{2}$ that relate to the geometries of the grid and rods. They can be found from Figures 18(a) and 18(b) in IEEE 80. However, for the cases considered their approximate values are $K_{1}=1.15$ and $K_{2}=4.75$. The apparent resistivity $\rho_{a}$ found from equation 46 in IEEE80 for the cases considered:-

$$
\rho_{a}=\frac{l_{r} \rho \rho_{s}}{\rho\left(h_{s}-h\right)+\rho_{s}\left(l_{r}+h-h_{r}\right)}=995.22 \mathrm{ohm}-\mathrm{m} .
$$



Figure H.1b Corner mesh potential versus the number of meshes.

If $\rho_{a}$ is calculated to be close to $\rho$ then take $\rho_{a}$ to equal $\rho$ as a conservative estimate, therefore $\rho_{a}=1000$ for this example.

Now find the total amount of material to be used in the grid and rods.
The total length $L_{r}$ of the ground rods is:-

$$
L_{r}=\left(N_{\mathrm{rod} 1}+N_{\mathrm{rod} 2}\right) l_{r}=200 \mathrm{~m}
$$

Note, let the total number of rods be $N_{\text {rod }}$ which equals $N_{\text {rod1 }}+N_{\text {rod2 }}$.
The total length $L_{g}$ of the grid conductors is:-

$$
L_{g}=2 n l_{\text {grid }}=120 \mathrm{~m}
$$

Where $l_{\text {grid }}=(n-1) d_{\text {sp }}$ is the buried length of one side of the grid, which is 10 m . The integer ' $n$ ' is the number of nodes on one side of the grid, or the number of meshes in one side plus 1.

The total length of buried rods and grid conductors including bonding connections is the weighted total $L_{c}$ :-

$$
L_{c}=L_{g}+1.15 L_{r}=350 \mathrm{~m}
$$

Having now obtained the lengths of rods and grid conductors it is now possible to calculate the ground resistance $R_{\text {ep }}$ using equations 41, 42, 43, 44 and 46 from sub-section 12.3 of IEEE80.

The following auxiliary equations are introduced to simplify the work involved:-

$$
\begin{array}{rlr}
U_{11} & =\frac{\rho_{s}}{\pi L_{g}} & =13.263 \\
h_{d} & =\sqrt{ }\left(d_{m} h\right) & =0.0707 \\
U_{12} & =\log _{e}\left(2 L_{g} / h_{d}\right) & =8.13 \\
U_{13} & =\frac{K_{1} L_{g}}{A^{0.5}} & =13.8 \\
U_{21} & =\frac{\rho_{a}}{2 \pi n l_{r}} & =0.531 \\
U_{22} & =\log _{e}\left(8 l_{r} / d_{r}\right) & =9.903 \\
U_{23} & =\frac{2 K_{1} l_{r}}{A^{0.5}} & =11.5 \\
U_{24} & =\left(n^{0.5}-1\right)^{2} & =2.101 \\
U_{31} & =\frac{\rho_{a}}{\pi L_{g}} & =2.653 \\
U_{32} & =\log _{e}\left(2 L_{g} / l_{r}\right) & =1.569
\end{array}
$$

Where $L_{g}=$ total length of the grid conductors
$l_{r}=$ average length of a buried rod, but in this example all the rods are the same length $h_{d}=$ weighted depth of the grid

Let

$$
\begin{aligned}
& R_{11}=\text { resistance of the grid conductors } \\
& R_{22}=\text { resistance of all the ground rods } \\
& R_{12}=\text { mutual resistance between the whole grid and all the rods }
\end{aligned}
$$

From equations 42, 43 and 44 from IEEE80, these resistances are: -

$$
\begin{array}{ll}
R_{11}=U_{11}\left(U_{12}+U_{13}-K_{2}\right) & =227.86 \mathrm{ohms} \\
R_{22}=U_{21}\left(U_{22}-1+\left(U_{23} U_{24}\right)\right) & =17.541 \mathrm{ohms} \\
R_{12}=U_{31}\left(U_{32}+U_{13}-K_{2}+1\right) & =30.82 \mathrm{ohms}
\end{array}
$$

From equation 41, for both the grid and the rods $R_{\text {ep }}$ becomes:-

$$
R_{\mathrm{ep}}=\frac{R_{1} R_{2}-R_{12}^{2}}{R_{1}+R_{2}-2 R_{12}}=16.582 \mathrm{ohms}
$$

Find the corner mesh voltage data.

Calculate the constants $K_{h}, K_{i i}$ and $K_{m}$ for use in equation 68 from IEEE80.

$$
K_{h}=(1+h)^{0.5}=1.2247
$$

Use the following auxiliary equations to simplify the work:-

$$
\begin{array}{ll}
U_{1}=\frac{d_{\mathrm{sp}}^{2}}{16 h d_{m}} & =50.0 \\
U_{2}=\frac{\left(d_{\mathrm{sp}}+2 h\right)^{2}}{8 d_{\mathrm{sp}} d_{m}} & =56.25 \\
U_{3}=\frac{h}{4 d_{m}} & =12.5 \\
U_{4}=\frac{8}{\pi(2 n-1)} & =0.2315 \\
U_{5}=\frac{K_{i i}}{K_{h}} & =0.8165
\end{array}
$$

Where $K_{i i}$ in this example is 1 .

$$
K_{m}=\frac{\log _{e}\left(U_{1}+U_{2}-U_{3}\right)+U_{5} \log _{e}\left(U_{4}\right)}{2 \pi}=0.5325
$$

Also from the explanation in sub-section 14.5.1 in IEEE80 the correction factor $K_{i}$ is required, which is:-

$$
K_{i}=0.656+0.172 N_{n}=1.688
$$

Where, $N_{n}=6$ - number of parallel conductors in each direction of the grid, which equals the number of nodes on each side of the grid.
$K_{h}=1.2247$ - correction factor for the depth of the grid.
$K_{i i}=1.0$ - correction factor if the rods are placed inside the grid area.
$K_{m}=0.5325-$ spacing factor for the mesh voltage.
$K_{i}=1.688$ - correction factor for the grid geometry as a function of the number of nodes on each side of the grid.

Having found $R_{\mathrm{ep}}, K_{m}$ and $K_{i}$ it is now possible to find the mesh voltage $E_{m}$ as follows. The resistance $R_{\text {ep }}$ is substituted into the fault current equations (H.1.1) and (H.1.2), to give the total fault current $I_{f}$. The earth return circuit between the pole at point A in Figure 13.12 and the earthing connection at point B at the source is a parallel circuit of the resistances to earth $R_{\text {en }}$ and $R_{\text {ep }}$ and the overhead earth return line impedance $Z_{\text {eoh }}$. The parallel combination is:-

$$
Z_{e}=\frac{Z_{\mathrm{eoh}}\left(R_{\mathrm{en}}+R_{\mathrm{ep}}\right)}{Z_{\mathrm{eoh}}+R_{\mathrm{en}}+R_{\mathrm{ep}}}=11.019+j 5.5597 \mathrm{ohms}
$$

Where

$$
Z_{\mathrm{eoh}}=\text { route length } \times Z_{0 \mathrm{pkm}}=10.5+j 22.5 \text { ohms }
$$

The proportion of current entering the ground $I_{\mathrm{fe}}$ is therefore:-

$$
\begin{aligned}
\left|I_{\mathrm{fe}}\right| & =\left|Z_{e} I_{f} /\left(R_{\mathrm{en}}+R_{\mathrm{ep}}\right)\right| \\
& =0.6826 \times 1057.4=721.74 \mathrm{amps}
\end{aligned}
$$

See Case C. 3 in Tables H.1c and H.1d.
The corner mesh voltage $E_{m}$ in the centre of the mesh at any corner of the grid is:

$$
E_{m}=\frac{\rho I_{\mathrm{fe}} K_{m} K_{i}}{L_{g}+1.15 L_{r}}=1853.6 \text { volts }
$$

Table H.1c. Data for earth resistance, touch voltage, ground potential rise and corner mesh voltage for different grid and rod designs

| Case | Resistivities |  | Area <br>  | $\rho$ | A | dr | hs | h | Nrod |
| :--- | ---: | ---: | ---: | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  | $l_{r}$ | $N_{\text {mesh }}$ |  |  |
| A.1 | 100 | 1000 | 36 | 0.02 | 0.2 | 0.5 | 2 | 10 | 3 |
| A.2 | 100 | 1000 | 64 | 0.02 | 0.2 | 0.5 | 2 | 10 | 4 |
| A.3 | 100 | 1000 | 100 | 0.02 | 0.2 | 0.5 | 4 | 10 | 5 |
| A.4 | 100 | 1000 | 144 | 0.02 | 0.2 | 0.5 | 4 | 10 | 6 |
| A.5 | 100 | 1000 | 196 | 0.02 | 0.2 | 0.5 | 5 | 10 | 7 |
| A.6 | 100 | 1000 | 256 | 0.02 | 0.2 | 0.5 | 5 | 10 | 8 |
| B.1 | 1000 | 5000 | 36 | 0.02 | 0.2 | 0.5 | 2 | 10 | 3 |
| B.2 | 1000 | 5000 | 64 | 0.02 | 0.2 | 0.5 | 2 | 10 | 4 |
| B.3 | 1000 | 5000 | 100 | 0.02 | 0.2 | 0.5 | 4 | 10 | 5 |
| B.4 | 1000 | 5000 | 144 | 0.02 | 0.2 | 0.5 | 4 | 10 | 6 |
| B.5 | 1000 | 5000 | 196 | 0.02 | 0.2 | 0.5 | 5 | 10 | 7 |
| B.6 | 1000 | 5000 | 256 | 0.02 | 0.2 | 0.5 | 5 | 10 | 8 |
| C.1 | 1000 | 5000 | 36 | 0.02 | 0.2 | 0.5 | 2 | 50 | 3 |
| C.2 | 1000 | 5000 | 64 | 0.02 | 0.2 | 0.5 | 2 | 50 | 4 |
| C.3 | 1000 | 5000 | 100 | 0.02 | 0.2 | 0.5 | 4 | 50 | 5 |
| C.4 | 1000 | 5000 | 144 | 0.02 | 0.2 | 0.5 | 4 | 50 | 6 |
| C.5 | 1000 | 5000 | 196 | 0.02 | 0.2 | 0.5 | 5 | 50 | 7 |
| C.6 | 1000 | 5000 | 256 | 0.02 | 0.2 | 0.5 | 5 | 50 | 8 |
| D.1 | 1000 | 5000 | 36 | 0.2 | 0.2 | 0.5 | 2 | 50 | 3 |
| D.2 | 1000 | 5000 | 64 | 0.2 | 0.2 | 0.5 | 2 | 50 | 4 |
| D.3 | 1000 | 5000 | 100 | 0.2 | 0.2 | 0.5 | 4 | 50 | 5 |
| D.4 | 1000 | 5000 | 144 | 0.2 | 0.2 | 0.5 | 4 | 50 | 6 |
| D.5 | 1000 | 5000 | 196 | 0.2 | 0.2 | 0.5 | 5 | 50 | 7 |
| D.6 | 1000 | 5000 | 256 | 0.2 | 0.2 | 0.5 | 5 | 50 | 8 |
| E.1 | 1000 | 5000 | 36 | 0.2 | 0.2 | 2.0 | 2 | 50 | 3 |
| E.2 | 1000 | 5000 | 64 | 0.2 | 0.2 | 2.0 | 2 | 50 | 4 |
| E.3 | 1000 | 5000 | 100 | 0.2 | 0.2 | 2.0 | 4 | 50 | 5 |
| E.4 | 1000 | 5000 | 144 | 0.2 | 0.2 | 2.0 | 4 | 50 | 6 |
| E.5 | 1000 | 5000 | 196 | 0.2 | 0.2 | 2.0 | 5 | 50 | 7 |
| E.6 | 1000 | 5000 | 256 | 0.2 | 0.2 | 2.0 | 5 | 50 | 8 |

Table H.1d. Results for earth resistance, touch voltage, ground potential rise and corner mesh voltage for different grid and rod designs

| Case | $R_{\text {ep }}$ | $E_{\text {touch50 }}$ | GPR | $E_{m}$ | $I_{\text {fe }}$ | $I_{f}$ |
| :--- | :---: | :---: | ---: | ---: | ---: | ---: |
| A.1 | 4.421 | 361 | 4796 | 1214 | 1085 | 1217 |
| A.2 | 3.716 | 361 | 4133 | 914 | 1112 | 1229 |
| A.3 | 3.215 | 361 | 3638 | 613 | 1132 | 1238 |
| A.4 | 2.838 | 361 | 5254 | 509 | 1147 | 1245 |
| A.5 | 2.544 | 361 | 2947 | 412 | 1158 | 1250 |
| A.6 | 2.307 | 361 | 2694 | 343 | 1168 | 1254 |
| B.1 | 44.13 | 1190 | 16,842 | 4271 | 382 | 929 |
| B.2 | 37.11 | 1190 | 16,161 | 3580 | 435 | 947 |
| B.3 | 32.12 | 1190 | 15,523 | 2618 | 483 | 964 |
| B.4 | 28.37 | 1190 | 14,936 | 2338 | 526 | 980 |
| B.5 | 25.43 | 1190 | 14,382 | 2009 | 565 | 995 |
| B.6 | 23.07 | 1190 | 13,862 | 1766 | 601 | 1008 |
| C.1 | 21.33 | 1190 | 13,431 | 3069 | 630 | 1020 |
| C.2 | 18.59 | 1190 | 12,644 | 2953 | 680 | 1040 |
| C.3 | 16.58 | 1190 | 11,968 | 1854 | 722 | 1057 |
| C.4 | 15.02 | 1190 | 11,373 | 1808 | 757 | 1072 |
| C.5 | 13.76 | 1190 | 10,841 | 1541 | 788 | 1085 |
| C.6 | 12.71 | 1190 | 10,360 | 1351 | 815 | 1097 |
| D.1 | 19.28 | 1190 | 12,856 | 3250 | 667 | 1035 |
| D.2 | 16.92 | 1190 | 12,087 | 3103 | 715 | 1054 |
| D.3 | 15.17 | 1190 | 11,433 | 1936 | 754 | 1071 |
| D.4 | 13.80 | 1190 | 10,861 | 1879 | 787 | 1085 |
| D.5 | 12.69 | 1190 | 10,351 | 1595 | 816 | 1097 |
| D.6 | 11.76 | 1190 | 10,043 | 1394 | 841 | 1108 |
| E.1 | 19.24 | 1190 | 12,947 | 3408 | 678 | 1035 |
| E.2 | 16.88 | 1190 | 12,073 | 3286 | 715 | 1054 |
| E.3 | 15.14 | 1190 | 11,421 | 2068 | 754 | 1071 |
| E.4 | 13.78 | 1190 | 10,851 | 2022 | 787 | 1085 |
| E.5 | 12.67 | 1190 | 10,343 | 1729 | 816 | 1098 |
| E.6 | 11.75 | 1190 | 9884 | 1521 | 841 | 1109 |
|  |  |  |  |  |  |  |

It is also necessary to relate the corner mesh voltage $E_{m}$ to the ground potential rise GPR of the grid and rod system.

$$
\mathrm{GPR}=I_{\mathrm{fe}} R_{\mathrm{ep}}=11967.9 \text { volts }
$$

Hence expressing $E_{m}$ as a percentage $\left(E_{\mathrm{mpc}}\right)$ of the GPR gives:-

$$
E_{\mathrm{mpc}}=\frac{E_{m} \times 100}{\mathrm{GPR}}=15.49 \%
$$

Comments on the results

Case A. The resistivity of the lower soil was chosen to be a moderate value of 100 ohm-m. Low values of resistance to earth at the pole, $R_{\mathrm{ep}}$, were easily obtained. The main criterion is that the corner mesh voltage $E_{m}$ must be less than the 50 kg touch voltage $E_{\text {touch } 50}$. Only one case A. 6 satisfies this criteria, 343 volts is less than 361 volts. This case requires a relatively large site area of $256 \mathrm{~m}^{2}$ for a pole and its associated equipment.

Case B. The resistivities were raised to values typical of dry and arid locations. In all cases the resistance to earth could not be reduced to 5 ohms. Again the 'mesh-touch' criteria could not be achieved. A satisfactory design could not be found.

Case C. The rods were driven deeper into the ground, to a depth of 50 m . The increase in depth by a factor of 5 only reduced the resistances to about $50 \%$ of their values in Case B. Some reduction in the corner mesh voltage was obtained.

Case D and E. Increasing the rod diameter by a factor of 10 and burying the grid deeper by a factor of 4 made very little difference to the results in Case C.

Necessary improvements.
In view of the difficulties found in providing a satisfactory solution, it would be advisable to include the 'ladder' network referred to in H. 1 and re-calculate the results. If this does not improve the situation significantly then two main improvements should be considered. Firstly use a neutral earth resistor at the source to restrict the earth return current to between 50 and 100 amps . This will directly reduce $E_{m}$ to values below $E_{\text {touch } 50}$. Secondly reduce the fault clearing time $t_{s}$ from 0.5 to 0.2 seconds. This may not be easily achieved. A sensitive earth current protective relay may need to be installed, e.g. core balance 51 N or 50 N relay. Reducing $t_{s}$ to 0.2 seconds will raise the $E_{\text {touch } 50}$ by a factor of 1.581 , which in Cases B to E causes $E_{\text {touch50 }}$ to become 1881 volts. This allows several of the cases to become feasible, e.g. B6, C3, C4, C5 and C6. The whole exercise should be repeated for other poles along the route so as to check whether or not a poorer situation could exist.

It may be noted that the simple treatment of the zero sequence impedances in the example would tend to be more appropriate to a remote switching station fed by an underground cable.

