## 32

## ECONOMICS AND FINANCE

### 32.1 INTRODUCTION

Chapter 32 is concerned with Economics and Finance. These two topics can ultimately dictate the decisions made by the practicing engineer and their company. For example, a company may decide that due to the rising price of their raw materials, they will explore the possibility of producing a raw material instead of purchasing it. A decision will then be based on whether it makes sense economically in the shortand long-term. Furthermore, economic evaluations are a major part of process and plant design.

This chapter provides introductory material to this vast field within engineering. The next section is devoted to definitions. This is followed with an overview of accounting principles. The chapter concludes with seven Illustrative Examples in the Applications section.

Both the qualitative and quantitative viewpoint is emphasized in this chapter although it is realized that the broad subject of engineering economics cannot be fitted into any rigid set of formulas. The material presented falls into roughly three parts: namely, general principles, practical information, and applications. The presentation starts with simple situations and proceeds to more complicated formulations and techniques that may be employed if there are sufficient data available. Other texts in the literature provide further details on the subject.

### 32.2 THE NEED FOR ECONOMIC ANALYSES

A company or individual hoping to increase its profitability must carefully assess a range of investment opportunities and select the most profitable options from those available. Increasing competitiveness also requires that efforts be expended to reducing costs of existing processes. In order to accomplish this, engineers should be fully aware of not only technical factors but also economic factors, particularly those that have the largest effect on profitability.

In earlier years, engineers concentrated on the technical side of projects and left the financial studies to the economist. In effect, engineers involved in making estimates of the capital and operating costs have often left the overall economic analysis and investment decision-making to others. This approach is no longer acceptable.

Some engineers are not equipped to perform a financial and/or economic analysis. Furthermore, many engineers already working for companies have never taken courses in this area. This shortsighted attitude is surprising in a group of people who normally go to great lengths to get all the available technical data before making an assessment of a project or study. The attitude is even more surprising when one notes that data are readily available to enable an engineer to assess the prospects of both his/her own company and those of his/her particular industry. ${ }^{(1)}$

As noted above, the purpose of this chapter is to provide a working tool to assist the student or engineer in not only understanding economics and finance but also in applying technical information to the economic design and operation of processes and plants. The material to follow will often focus on industrial and/or plant applications. Hopefully, this approach will provide the reader with a better understanding of some of the fundamentals and principles.

Bridging the gap between theory and practice is often a matter of experience acquired over a number of years. Even then, methods developed from experience all too often must be re-evaluated in the light of changing economic conditions if optimum designs are to result. The approach presented here therefore represents an attempt to provide a consistent and reasonably concise method for the solution of these problems involving economic alternatives. ${ }^{(2)}$

The term "economic analysis" in engineering problems generally refers to calculations made to determine the conditions for realizing maximum financial return for a design or operation. The same general principles apply, whether one is interested in the choice of alternatives for completing projects, in the design of plants so that the various components are economically proportioned, or in the technique of economical operation of existing plants. General considerations that form the framework on which sound decisions must be made are often simple. Sometimes their application to the problems encountered in the development of a commercial enterprise involves too many intangibles to allow exact analysis, in which case judgment must be intuitive. Often, however, such calculations may be made with a considerable degree of exactness. This chapter will attempt to develop a relatively concise method for applying these principles.

Finally, concern with maximum financial return implies that the criterion for judging projects involved is profit. While this is usually true, there are many
important objectives which, though aimed at ultimate profit increase, cannot be immediately evaluated in quantitative terms. Perhaps the most significant of these is increased concern with environmental degradation and sustainability. Thus, there has been some tendency in recent years to regard management of commercial organizations as a profession with social obligations and responsibilities; considerations other than the profit motive may govern business decisions. However, these additional social objectives are for the most part often not inconsistent with the economic goal of satisfying human wants with the minimum effort. In fact, even in the operation of primarily nonprofit organizations, it is still important to determine the effect of various policies on profit. ${ }^{(2)}$

The next section is devoted to definitions. This is followed with an overview of accounting principles and applications. This chapter concludes with applications.

### 32.3 DEFINITIONS

Before proceeding to the applications, it would be wise to provide the reader with certain key definitions in the field. Fourteen concepts that often come into play in an economic analysis are given below. The definitions have been drawn from the literature. ${ }^{(3)}$

### 32.3.1 Simple Interest

The term interest can be defined as the money paid for the use of money. It is also referred to as the value or worth of money. Two terms of concern are simple interest and compound interest. Simple interest is always computed on the original principal. The basic formula to employ in simple interest calculations is:

$$
\begin{equation*}
S=P(1+n i) \tag{32.1}
\end{equation*}
$$

```
where \(P=\) original principal
    \(n=\) time in years
    \(i=\) annual interest rate
    \(S=\) sum of interest and principal after \(n\) years
```

Normally, the interest period is one year, in which case $i$ is referred to as the effective interest rate.

### 32.3.2 Compound Interest

Unlike simple interest, with compound interest, interest is added periodically to the original principal. The term conversion or compounding of interest simply refers to the addition of interest to the principal. The interest period or conversion period in compound interest calculations is the time interval between successive conversions of interest and the interest period is the ratio of the stated annual rate to this
number of interest periods in one year. Thus, if the given interest rate is $10 \%$ compounded semiannually, the interest period is 6 months and the interest rate per interest period is $5 \%$. Alternately, if the given interest rate is $10 \%$ compounded quarterly, then the interest period is 3 months and the interest rate per interest period is $2.5 \%$. One should always assume the interest is compounded annually unless otherwise stated. The basic formula to employ for compound interest is:

$$
\begin{equation*}
S=P(1+i)^{n} \tag{32.2}
\end{equation*}
$$

If interest payments become due $m$ times per year at compound interest, $(m)(n)$ payments are required in $n$ years. A nominal annual interest rate, $i^{\prime}$, may be defined by:

$$
\begin{equation*}
S=P\left(1+\frac{i^{i}}{m}\right)^{m n} \tag{32.3}
\end{equation*}
$$

In this case, the effective annual interest, $i$, is:

$$
\begin{equation*}
i=\left(1+\frac{i^{\prime}}{m}\right)^{m}-1 \tag{32.4}
\end{equation*}
$$

In the limit (as $m$ approaches infinity), such payments may be considered to be required at infinitesimally short intervals, in which case, the interest is said to be compounded continuously. Numerically, the difference between continuous and annual compounding is small. However, annual compounding may be significant when applied to very large sums of money.

### 32.3.3 Present Worth

The present worth is the current value of a sum of money due at time $n$ and at interest rate $i$. This equation is the compound interest equation solved for the present worth term, $P$

$$
\begin{equation*}
P=S(1+i)^{-n} \tag{32.5}
\end{equation*}
$$

### 32.3.4 Evaluation of Sums of Money

The value of a sum of money changes with time because of interest considerations. $\$ 1000$ today, $\$ 1000$ ten years from now, and $\$ 1000$ ten years ago all have different meanings when interest is taken into account. $\$ 1000$ today would be worth more ten years from now because of the interest that could be accumulated in the interim. On the other hand, $\$ 1000$ today would have been worth less ten years ago because a smaller sum of money could have been invested then so as to yield $\$ 1000$ today. Therefore, one must refer to the date as well as the sum of money.

Summarizing, evaluating single sums of money requires multiplying by $(1+i)^{n}$ if the required date of evaluation is after the date associated with the obligation or
multiplying by $(1+i)^{-n}$ if the required date of evaluation is before the date associated with the obligation. The term $n$ is always the time in periods between the date associated with the obligation and the date of evaluation.

The evaluation of sums of money may be applied to the evaluation of a uniform series of payments. A uniform series is a series of equal payments made at equal intervals. Suppose $R$ is invested at the end of every interest period for $n$ periods. The total value of all these payments, $S$, as of the date of the last payment, may be calculated from the equation

$$
\begin{equation*}
S=R\left[(1+i)^{n}-1\right] / i \tag{32.6}
\end{equation*}
$$

The term $S$ is then called the amount of the uniform series.

### 32.3.5 Depreciation

The term depreciation refers to the decrease in the value of an asset. Two approaches that can be employed are the straight line and sinking fund method. In the straight line method of depreciation, the value of the asset is decreased each year by a constant amount. The annual depreciation amount, $D$, is given by

$$
\begin{equation*}
D=(\text { Original cost }- \text { Salvage value }) /(\text { Estimated life in years }) \tag{32.7}
\end{equation*}
$$

In the sinking fund method of depreciation, the value of the asset is determined by first assuming that a sinking fund consisting of uniform annual payments had been set up for the purpose of replacing the asset at the end of its estimated life. The uniform annual payment (UAP) may be calculated from the equation

$$
\mathrm{UAP}=(\text { Original cost }- \text { Salvage value })(\mathrm{SFDF})
$$

where SFDF is the sinking fund deposit factor and is given by

$$
\begin{equation*}
\mathrm{SFDF}=i /\left[(1+i)^{n}-1\right] \tag{32.8}
\end{equation*}
$$

The value of the asset at any time is estimated to be the difference between the original cost and the amount that would have accumulated in the sinking fund. The amount accumulated in the sinking fund is obtained by multiplying the SFDF by the compound amount factor (CAF) where

$$
\begin{equation*}
\mathrm{CAF}=\left[(1+i)^{n}-1\right] / i \tag{32.9}
\end{equation*}
$$

### 32.3.6 Fabricated Equipment Cost Index

A simple process is available to estimate the equipment cost from past cost data. The method consists of adjusting the earlier cost data to present values using factors that correct for inflation. A number of such indices are available; one of the most
commonly used is the fabricated equipment cost index (FECI)

$$
\begin{equation*}
\operatorname{Cost}_{y \text { ear } B}=\operatorname{Cost}_{y e a r} \mathrm{~A}\left(\frac{\mathrm{FECI}_{\text {year } B}}{\mathrm{FECI}_{\text {year } \mathrm{A}}}\right) \tag{32.10}
\end{equation*}
$$

Given the cost and FECI for year A, as well as the FECI for year B, the cost of the equipment in year $B$ can be estimated.

### 32.3.7 Capital Recovery Factor

In comparing alternative processes or different options for a particular process from an economic point-of-view, one recommended procedure to follow is that the total capital cost can be converted to an annual basis by distributing it over the projected lifetime of the facility (or the equivalent). The sum of both the annualized capital cost (ACC), including installation, and the annual operating cost (AOC), is called the total annualized cost (TAC) for the project or facility. The economic merit of the proposed facility, process, or scheme can be examined once the total annual cost is available.

The conversion of the total capital cost (TCC) to an ACC requires the determination of an economic parameter known as the capital recovery factor (CRF). This parameter can be found in any standard economics textbook or calculated directly from the following equation:

$$
\begin{equation*}
\mathrm{CRF}=i(1+i)^{n} /\left[(1+i)^{n}-1\right] \tag{32.11}
\end{equation*}
$$

where $n=$ projected lifetime of the system,
$i=$ annual interest rate (as a fraction).

The CRF is a positive, fractional number. Once this factor has been determined, the ACC can be calculated from the following equation:

$$
\begin{equation*}
\mathrm{ACC}=(\mathrm{TCC})(\mathrm{CRF}) \tag{32.12}
\end{equation*}
$$

The annualized capital cost reflects the cost associated with recovering the initial capital expenditure over the depreciable life of the system.

### 32.3.8 Present Net Worth

There are various approaches that may be employed in the economic selection of the best of several alternatives. For each alternative in the present net worth (PNW) method of economic selection, the single sum is calculated that would provide for all expenditures over a common time period. The alternative having the least PNW of expenditures is selected as the most economical. The equation to employ is

$$
\begin{equation*}
\mathrm{PNW}=\mathrm{CC}+\mathrm{PN}+\mathrm{PWD}-\mathrm{PWS} \tag{32.13}
\end{equation*}
$$

where $\mathrm{CC}=$ Capital cost,
$\mathrm{PN}=$ Future renewals,
PWD $=$ Other disbursements, $\mathrm{PWS}=$ Salvage value.

If the estimated lifetimes differ for the various alternatives, employ a period of time equal to the least common multiple of the different lifetimes for renewal purposes.

### 32.3.9 Perpetual Life

Capitalized cost can be viewed as present worth under the assumption of perpetual life. Computing capitalized cost involves, in a very real sense, finding the present worth of an infinite series of payments. To obtain the present worth of an infinite series of payments of $\$ R$ at the end of each interest period forever, one needs simply to divide $R$ by $i$, where $i$ is the interest rate per interest period. Thus, to determine what sum of money, $P$, would have to be invested at $8.0 \%$ to provide payments of $\$ 100,000$ at the end of each year forever, $P$, would have to be such that the interest on it each period would be $\$ 100,000$. Withdrawal of the interest at the end of each period would leave the original sum intact to again draw $\$ 100,000$ interest at the end of the next period. For this example,

$$
\begin{aligned}
P & =100,000 / 0.08 \\
& =\$ 1,250,000
\end{aligned}
$$

The $\$ 1,250,000$ would be the present worth of an infinite series of payments of $\$ 100,000$ at the end of each year forever, assuming money is worth $8 \%$.

To determine the present worth of an infinite series of payments of $\$ R$ at the end of each $n$ periods forever, first multiply by the SFDF to convert to an equivalent single period payment and then divide by $i$ to obtain the present worth.

### 32.3.10 Break-Even Point

From an economic point-of-view, the break-even point of a process operation is defined as that condition when the costs $(C)$ exactly balance the income ( $I$ ). The profit ( $P$ ) is therefore,

$$
\begin{equation*}
P=I-C \tag{32.14}
\end{equation*}
$$

At break-even, the profit is zero.

### 32.3.11 Approximate Rate of Return

Rate of return can be viewed as the interest that will make the present worth of net receipts equal to the investment. The approximate rate of return (ARR), denoted
by some as $p$, may be estimated from the equation below:

$$
\begin{equation*}
p=\text { ARR }=\text { Average annual profit or earnings/Initial total investment } \tag{32.15}
\end{equation*}
$$

To determine the average annual profit, simply divide the difference between the total money receipts (income) and the total money disbursements (expenses) by the number of years in the period of the investment.

### 32.3.12 Exact Rate of Return

Using the approximate rate of return as a guide, one can generate the exact rate of return (ERR). This is usually obtained by trial-and-error and interpolation calculations of the rate of interest that makes the present worth of net receipts equal to the investment. The approximate rate of return will tend to overestimate the exact rate of return when all or a large part of the receipts occur at the end of a period of investment. The approximate rate will tend to underestimate the exact rate when the salvage value is zero and also when the salvage value is a high percentage of the investment.

### 32.3.13 Bonds

A bond is a written promise to pay both a certain sum of money (redemption price) at a future date (redemption date) and equal interest payments at equal intervals in the interim. The holder of a $\$ 1000,5 \%$ bond, redeemable at 105 (bond prices are listed without the last zero) in 10 years, with interest payable semiannually would be entitled to semiannual payments of $\$ 1000(0.25)$ or $\$ 25$ for 10 years and $105 \%$ of $\$ 1000$, that is $\$ 1050$, at the end of 10 years when the bond is redeemed.

The interest payment on a bond is found by multiplying the face value of the bond by the bond interest rate per period. From above, the face value is $\$ 1000$ and the bond interest rate per period is 0.025 . Therefore, the periodic interest payment is $\$ 25$. Redeemable at 105 means that the redemption price is $105 \%$ of the face value of the bond.

The purchase price of a bond depends on the yield rate, that is the actual rate of return on the investment represented by the bond purchase. Therefore, the purchase price of a bond is the present worth of the redemption price plus the present worth of future interest payments, all computed at the yield rate. The bond purchase price formula is:

$$
\begin{equation*}
V=C(1+i)^{-n}+R\left[1-(1+i)^{-n}\right] / i \tag{32.16}
\end{equation*}
$$

```
where \(V=\) purchase price,
\(C=\) redemption price,
\(R=\) periodic interest payment,
\(n=\) time in periods to maturity,
\(i=\) yield rate.
```


### 32.3.14 Incremental Cost

By definition, the average unit increment cost is the increase in cost divided by the increase in production. Only those cost factors which vary with production can affect the average unit increment cost. In problems involving decisions as to whether to stay in production or (temporarily) shut down, the average unit increment cost may be compared with the unit increment cost or the unit selling price.

### 32.4 PRINCIPLES OF ACCOUNTING ${ }^{(3)}$

Accounting is the science of recording business transactions in a systematic manner. Financial statements are both the basis for and the result of management decisions. Such statements can tell a manager or an engineer a great deal about a company, provided that one can interpret the information correctly.

Since a fair allocation of costs requires considerable technical knowledge of operations in the chemical process industries, a close liaison between the senior process engineers and the accountants in a company is desirable. Indeed, the success of a company depends on a combination of financial, technical and managerial skills.

Accounting is also the language of business and the different departments of management use it to communicate within a broad context of financial and cost terms. The engineer who does not take the trouble to learn the language of accountancy denies himself the most important means available for communicating with top management. He may be thought by them to lack business acumen. Some engineers have only themselves to blame for their lowly status within the company hierarchy since they seem determined to hide themselves from business realities behind the screen of their specialized technical expertise. However, more and more engineers are becoming involved in decisions that are business related.

Engineers involved in feasibility studies and detailed process evaluations are dependent on financial information from the company accountants, especially information regarding the way the company intends to allocate its overhead costs. It is vital that the engineer should correctly interpret such information and that he/she can, if necessary, make the accountant understand the effect of the chosen method of allocation.

The method of allocating overheads can seriously affect the assigned costs of a project and hence the apparent cash flow for that project. Since these cash flows are often used to assess profitability by such methods as PNW, unfair allocation of overhead costs can result in a wrong choice between alternative projects.

In addition to understanding the principles of accountancy and obtaining a working knowledge of its practical techniques, the engineer should be aware of possible inaccuracies of accounting information in the same way that he/she allows for errors in any technical data.

At first acquaintance, the language of accountancy appears illogical to most engineers. Although the accountant normally expresses information in tabular form, the basis of all practice can be simply expressed by:

$$
\begin{equation*}
\text { Capital }=\text { Assets }- \text { Liabilities } \tag{32.17}
\end{equation*}
$$

or

$$
\begin{equation*}
\text { Assets }=\text { Capital }+ \text { Liabilities } \tag{32.18}
\end{equation*}
$$

Capital, often referred to as net worth, is the money value of the business, since assets are the money values of things the business owns while liabilities are the money value of the things the business owes.

Most engineers have great difficulty in thinking of capital (also known as ownership) as a liability. This is easily overcome once it is realized that a business is a legal entity in its own right, owing money to the individuals who own it. This realization is absolutely essential when considering large companies with stockholders, and is used for consistency even for sole ownerships and partnerships. If a person (say LT) puts up $\$ 10,000$ capital to start a business, then that business has a liability to repay $\$ 10,000$ to that person.

It is even more difficult to think of profit as being a liability. Profit is the increase in money available for distribution to the owners, and effectively represents the interest obtained on the capital. If the profit is not distributed, it represents an increase in capital by the normal concept of compound interest. Thus, if the business makes a profit of $\$ 5000$, the liability is increased to $\$ 15,000$. With this concept in mind Equation (32.18) can be expanded to:

$$
\begin{equation*}
\text { Assets }=\text { Capital }+ \text { Liabilities }+ \text { Profit } \tag{32.19}
\end{equation*}
$$

where the capital is considered as the cash investment in the business and is distinguished from the resultant profit in the same way that principal and interest are separated.

Profit (as referred to above) is the difference between the total cash revenue from sales and the total of all costs and other expenses incurred in making those sales. With this definition, Equation (32.19) can be further expanded to:

$$
\begin{align*}
\text { Assets }+ \text { Expenses }= & \text { Capital }+ \text { Liabilities }+ \text { Profit } \\
& + \text { Revenue from sales } \tag{32.20}
\end{align*}
$$

Some engineers have the greatest difficulty in regarding an expense as being equivalent to an asset, as is implied by Equation (32.20). However, consider LT's earnings. During the period in which he made a profit of $\$ 5000$, his total expenses excluding his earnings were $\$ 8000$. If he assessed the worth of his labor to the business at $\$ 12,000$, then the revenue required from sales would be $\$ 25,000$. Effectively, LT has made a personal income of $\$ 17,000$ in the year but he has apportioned it to the business as $\$ 12,000$ expense for his labor and $\$ 5000$ return on his capital. In larger businesses, there will also be those who receive salaries but do not hold stock and therefore, receive no profits, and stockholders who receive profits but no salaries. Thus, the difference between expenses and profits is very practical.

The period covered by the published accounts of a company is usually one year, but the details from which these accounts are compiled are often entered daily in a
journal. The journal is a chronological listing of every transaction of the business, with details of the corresponding income or expenditure. For the smallest businesses, this may provide sufficient documentation but, in most cases, the unsystematic nature of the journal can lead to computational errors. Therefore, the usual practice is to keep accounts that are listings of transactions related to a specific topic such as "Purchase of Oil Account." This account would list the cost of each purchase of oil, together with the date of purchase, as extracted from the journal.

The traditional work of accountants has been to prepare balance sheets and income statements. Nowadays, accountants are becoming increasingly concerned with forward planning. Modern accountancy can roughly be divided into two branches: financial accountancy and management or cost accountancy.

Financial accountancy is concerned with stewardship. This involves the preparation of balance sheets and income statements that represent the interest of stockholders and are consistent with the existing legal requirements. Taxation is an important element of financial accounting.

Management accounting is concerned with decision-making and control. This is the branch of accountancy closest to the interest of most (process) engineers. Management accounting is concerned with standard costing, budgetary control, and investment decisions.

Accounting statements only present facts that can be expressed in financial terms. They do not indicate whether a company is developing new products that will ensure a sound business future. A company may have impressive current financial statements and yet may be heading for bankruptcy in a few years' time if provision is not being made for the introduction of sufficient new products or services.

### 32.5 APPLICATIONS

The remainder of the chapter is devoted to Illustrative Examples, many of which contain technical developmental material. A good number of fluid flow related applications have been drawn from the National Science Foundation (NSF) literature ${ }^{(4-8)}$ and two other key sources. ${ }^{(9,10)}$

Illustrative Example 32.1 List the major fixed capital costs for the chemical process industry.

## Solution

1. Major process equipment (i.e., reactors, tanks, pumps, filters, distillation columns, etc.).
2. Installation of major process equipment.
3. Process piping.
4. Insulation.
5. Instrumentation.
6. Auxiliary facilities (i.e., power substations, transformers, boiler houses, firecontrol equipment, etc.).
7. Outside lines (i.e., piping external to buildings, supports and posts for overhead piping, electric feeders from power substations, etc.).
8. Land and site improvements.
9. Building and structures.
10. Consultant fees.
11. Engineering and construction (design and engineering fees plus supervision of plant erection).
12. Contractors' fees (administrative).

Illustrative Example 32.2 List the major working capital costs for the chemical process industry.

## Solution

1. Raw materials for plant startup.
2. Raw material, intermediate and finished product inventories.
3. Cost of handling and transportation of materials to and from sites.
4. Cost inventory control, warehouse, associated insurance, security arrangements, etc.
5. Money to carry accounts receivable (i.e., credit extended to customers) less accounts payable (i.e., credit extended by suppliers).
6. Money to meet payrolls when starting up.
7. Readily available cash for emergency.
8. Any additional cash required to operate the process or business.
9. Expenses associated with new hirees.
10. Startup consultant fees.

Illustrative Example 32.3 Answer the following three questions:

1. Define the straight-line method of analysis that is employed in calculating depreciation allowances.
2. Define the double-declining balance (DDB) method of analysis.
3. Define the sum-of-the-year's digits (SYD) method of analysis.

Solution The straight-line rate of depreciation is a constant equal to $1 / r$, where $r$ is the life of the facility for tax purposes. Thus, if the life of the plant is 10 yr , the straight-line rate of depreciation is 0.1 . This rate, applied over each of the 10 yr , will result in a depreciation reserve equal to the initial investment.

A declining balance rate is obtained by first computing the straight-line rate and then applying some multiple of that rate to each year's unrecovered cost rather
than to the original investment. Under the double-declining balance method, twice the straight-line rate is applied to each year's remaining unrecovered cost. Thus, if the life of a facility is 10 years, the straight-line rate will be 0.1 , and the first year's double-declining balance will be 0.2 . If the original investment is $I$, the depreciation allowance the first year will be $0.2 I$. For the second year, it will be $0.16 I$, or 0.2 of the unrecovered cost of 0.81 . The depreciation allowances for the remaining years are calculated in a similar manner until the tenth year has been completed. Since this method involves taking a fraction of an unrecovered cost each year, it will never result in the complete recovery of the investment. To overcome this objection, the U.S. Internal Revenue Service (IRS) allowed the taxpayer in the past to shift from the DDB depreciation method to the straight-line method any time after the start of the project.

The rate of depreciation for the sum-of-the-year's digits method is a fraction. The numerator of this fraction is the remaining useful life of the property at the beginning of the tax year, while the denominator is the sum of the individual digits corresponding to the total years of life of the project. Thus, with a project life, $r$, of 10 years, the sum of the year's digits will be $10+9+8+7+6+5+4+3+2+1=55$. The depreciation rate the first year will be $10 / 55=0.182$. If the initial cost of the facility is $I$, the depreciation for the first year will be $0.182 I, 9 / 55=0.164 I$ for the second year, and so on until the last year. The SYD method will recover $100 \%$ of the investment at the end of $r$ years. A shift from SYD to straight-line depreciation cannot be made once the SYD method has been started.

Illustrative Example 32.4 Compare the results of the three methods discussed in Illustrative Example 32.3.

Solution A tabular summary of the results of depreciation according to the straightline, double-declining, and sum-of-the-year's digits methods are shown in Table 32.1.

Table 32.1 Comparative methods of analysis

| Year | Straight-Line | Double-Declining | Sum-of-the-Year's Digits |
| :--- | :---: | :---: | :---: |
| 0 | 1.000 | 1.000 | 1.000 |
| 1 | 0.900 | 0.800 | 0.818 |
| 2 | 0.800 | 0.640 | 0.655 |
| 3 | 0.700 | 0.512 | 0.510 |
| 4 | 0.600 | 0.410 | 0.383 |
| 5 | 0.500 | 0.328 | 0.274 |
| 6 | 0.400 | 0.262 | 0.183 |
| 7 | 0.300 | 0.210 | 0.110 |
| 8 | 0.200 | 0.168 | 0.056 |
| 9 | 0.100 | 0.134 | 0.018 |
| 10 | 0.000 | 0.108 | 0.000 |

Illustrative Example 32.5 A fluid is to be transported 4 miles under turbulent flow conditions. An engineer is confronted with two choices in designing the system:
A. Employ a 2 inch ID pipe at a cost of $\$ 1 /$ foot.
B. Employ a 4 inch ID pipe at a cost of $\$ 6 /$ foot.

Pressure drop costs for the 2 inch ID pipe are $\$ 20,000 / \mathrm{yr}$. Assume only that the operating cost is the pressure drop and the only capital cost is the pipe. The capital recovery factor (CRF) for either pipe system is 0.1. Estimate the operating cost for the 4 inch ID pipe. Also determine which is the more economical pipe system?

Solution The pressure drop is (approximately) proportional to the velocity squared for turbulent flow. The velocity of the fluid is lower for the 4-inch ID pipe. Since the area ratio is 4 (diameter squared), the 4 -inch ID pipe velocity is one quarter of the velocity of the fluid in the 2-inch ID pipe. Therefore, the pressure drop for 4 -inch ID pipe is approximately one sixteenth of the pressure drop for 2-inch ID pipe. The operating cost associated with the pressure drop cost is equal to:

$$
\text { Operating cost }=\frac{\$ 20,000 / \mathrm{yr}}{16}=\$ 1250 / \mathrm{yr} ; \quad 2 \text {-inch ID pipe }
$$

To select the more economic pipe system, calculate the total cost

$$
\text { Total cost }=\text { Operating cost }+ \text { Capital cost }
$$

The operating cost for a 2 -inch pipe system and a 4 -inch pipe system are given in the problem statement and calculated above, respectively. The annual capital cost is calculated as follows:

$$
\begin{aligned}
\text { Capital cost } & =(\text { Distance })(\text { Cost })(\text { Capital recovery factor }) \\
\text { Capital cost }(2 \text { inch }) & =(4 \text { miles })(5280 \mathrm{ft} / \text { mile })(\$ 1 / \mathrm{ft})(0.1)=\$ 2110 \\
\text { Capital cost }(4 \mathrm{inch}) & =(4 \text { miles })(5280 \mathrm{ft} / \text { mile })(\$ 6 / \mathrm{ft})(0.1)=\$ 12,700
\end{aligned}
$$

Annual data is summarized in Table 32.2. Obviously, the 4-inch pipe is more economical.

Table 32.2 Cost results for two different sized pipes

|  | 2 inch | 4 inch |
| :--- | :--- | :--- |
| Operating cost | $\$ 20,000$ | $\$ 1250$ |
| Capital cost | $\$ 2110$ | $\$ 12,700$ |
| Total cost | $\$ 22,110$ | $\$ 13,950$ |

Illustrative Example 32.6 A process emits $50,000 \mathrm{acfm}$ of gas containing a dust (it may be considered ash and/or metal) at a loading of $2.0 \mathrm{gr} / \mathrm{ft}^{3}$. A particulate control device is employed for particle capture and the dust captured from the unit is worth
$\$ 0.03 / \mathrm{lb}$ of dust. Experimental data have shown that the collection efficiency, $E$, is related to the system pressure drop, $\Delta P$, by the formula:

$$
E=\frac{\Delta P}{\Delta P+15.0}
$$

where $E=$ fractional collection efficiency, $\Delta P=$ pressure drop, $\mathrm{lb}_{\mathrm{f}} / \mathrm{ft}^{2}$.

If the fan is $55 \%$ efficient (overall) and electric power costs $\$ 0.18 / \mathrm{kW} \cdot \mathrm{h}$, at what collection efficiency is the cost of power equal to the value of the recovered material? What is the pressure drop in inches of water (in $\mathrm{H}_{2} \mathrm{O}$ ) at this condition?

Solution The value of the recovered material (RV) may be expressed in terms of the fractional collection efficiency $E$, the volumetric flowrate $q$, the inlet dust loading $c$, and the value of the dust (DV):

$$
\mathrm{RV}=(q)(c)(\mathrm{DV})(E)
$$

Substituting yields

$$
\mathrm{RV}=\left(\frac{50,000 \mathrm{ft}^{3}}{\min }\right)\left(\frac{2.0 \mathrm{gr}}{\mathrm{ft}^{3}}\right)\left(\frac{1 \mathrm{lb}}{7000 \mathrm{gr}}\right)\left(\frac{0.03 \$}{\mathrm{lb}}\right)(E)=0.429 E \$ / \mathrm{min}
$$

The recovered value can be expressed in terms of pressure drop, that is, replace $E$ by $\Delta P$ :

$$
\mathrm{RV}=\frac{(0.429)(\Delta P)}{\Delta P+15.0} \$ / \mathrm{min}
$$

The cost of power (CP) in terms of $\Delta P, q$, the cost of electricity (CE) and the fan fractional efficiency, $E_{f}$, is

$$
\mathrm{CP}=(q)(\Delta P)(\mathrm{CE}) /\left(E_{f}\right)
$$

Substitution yields

$$
\begin{aligned}
\mathrm{CP} & =\left(\frac{50,000 \mathrm{ft}^{3}}{\mathrm{~min}}\right)\left(\frac{\Delta P \mathrm{lb}_{\mathrm{f}}}{\mathrm{ft}^{2}}\right)\left(\frac{0.18 \$}{\mathrm{~kW} \cdot \mathrm{~h}}\right)\left(\frac{1 \mathrm{~min} \cdot \mathrm{~kW}}{44,200 \mathrm{ft} \cdot \mathrm{lb}_{\mathrm{f}}}\right)\left(\frac{1}{0.55}\right)\left(\frac{1 \mathrm{~h}}{60 \mathrm{~min}}\right) \\
& =0.006 \Delta P \$ / \mathrm{min}
\end{aligned}
$$

The pressure drop at which the cost of power is equal to the value of the recovered material is found by equating RV with CP:

$$
\begin{aligned}
\mathrm{RV} & =\mathrm{CP} \\
\Delta P & =66.5 \mathrm{lb}_{\mathrm{f}} / \mathrm{ft}^{2} \\
& =12.8 \mathrm{in} . \mathrm{H}_{2} \mathrm{O}
\end{aligned}
$$

Figure 32.1 shows the variation of $\mathrm{RV}, \mathrm{CP}$, and profit with pressure drop.
The collection efficiency corresponding to the above calculated $\Delta P$ is

$$
\begin{aligned}
E & =\frac{\Delta P}{\Delta P+15.0} \\
& =\frac{66.5}{66.5+15.0} \\
& =0.82 \\
& =82.0 \%
\end{aligned}
$$

The reader should note that operating below this efficiency (or the corresponding pressure drop) will produce a profit; operating above this value leads to a loss.

The operating condition for maximum profit can be estimated from Fig. 32.1. Calculating this value is left as an exercise for the reader. [Hint: Set the first derivative of the profit (i.e., $\mathrm{RV}-\mathrm{CP}$ ) with respect to $\Delta P$ equal to zero. The answer is $13.9 \mathrm{lb}_{\mathrm{f}} / \mathrm{ft}^{2}$.]

Illustrative Example 32.8 A filter press costing $\$ 60,000$ has an estimated lifetime of 9 years and a salvage value of $\$ 500$. What uniform annual payment must be made


Figure 32.1 Profit as a function of pressure drop.
into a fund at the end of the year to replace the press if the fund earns $3.375 \%$ ? What would be the appraisal value of the press at the end of the fifth year based on straight line depreciation?

Solution Write the equation for the uniform annual payment (UAP) in terms of the cost ( $P$ ) and salvage value ( $L$ ), using a sinking fund model. See Equation (32.8).

$$
\mathrm{UAP}=(P-L)(\mathrm{SFDF})
$$

Calculate the sinking fund depreciation factor, SFDF

$$
\mathrm{SFDF}=\frac{i}{(1+i)^{n}-1}=\frac{0.03375}{(1+0.03375)^{9}-1}=0.0969
$$

Thus,

$$
\mathrm{UAP}=(\$ 60,000-\$ 500)(0.0969)=\$ 5765
$$

In determining the appraisal value where the straight line method of depreciation is used, the following equation applies:

$$
B=P-\left(\frac{P-L}{n}\right) x
$$

The term $n$ refers to the years to the end of life, and $x$ refers to any time from the present before the end of usable life. Employ this equation for the appraisal value and solve for $B_{5}$ after 5 years

$$
B_{5}=\$ 60,000-\left(\frac{\$ 60,000-\$ 500}{9}\right)(5)=\$ 26,945
$$

This problem assumed that the depreciation of the filter press followed a sinking fund method, while the appraisal value of the press followed a straight line depreciation trend. For the depreciation calculation, it is assumed that the press will remain in operation for all of its 9 years of usable life. For this reason, the depreciable amount of the press may be thought of as being deposited into a sinking fund to be applied toward the replacement of the press after nine years.

The appraisal value of the press after the fifth year is calculated as part of the appraisal calculation. This value takes into account the fact that the press, even one year after it is purchased, is no longer worth what was paid for it. Since the appraisal had little to do with the fund for its replacement, the press was assumed to follow a straight line depreciation model.

Illustrative Example 32.9 The annual operation costs of an outdated environmental control device is $\$ 75,000$. Under a proposed emission reduction plan, the installation of a new fan system will require an initial cost of $\$ 150,000$ and an annual operating cost of $\$ 15,000$ for the first 5 years. Determine the annualized cost for the new processing system by assuming the system has only 5 years ( $n$ )
operational life. The interest rate (i) is $7 \%$. The capital recovery factor (CRF) or annual payment of a capital investment can be calculated as follows:

$$
\mathrm{CRF}=\left(\frac{A}{P}\right)_{i, n}=\frac{i(1+1)^{n}}{(1+i)^{n}-1}
$$

where $A$ is the annual cost and $P$ is the present worth.
Compare the costs for both the outdated and proposed operations.

Solution The annualized cost for the new fan is determined based on the following input data:

Capital cost $=\$ 150,000$
Interest, $i=7 \%$
Term, $n=5 \mathrm{yr}$

For $i=0.07$ and $n=5$, the CRF is

$$
\begin{aligned}
\mathrm{CRF} & =\frac{0.07(1+0.07)^{5}}{(1+0.07)^{5}-1} \\
& =0.2439
\end{aligned}
$$

The total annualized cost for the fan is then

$$
\begin{aligned}
\text { Annualized cost } & =\text { Installation cost }+ \text { Operation cost } \\
& =(0.2439)(\$ 150,000)+\$ 15,000=\$ 51,585
\end{aligned}
$$

Since this cost is lower than the annual cost of $\$ 75,000$ for the old process, the proposed plan should be substituted.

## REFERENCES

1. F. Holland, F. Watson, and J. Wilkinson, "Financing Assets by Equity and Debt," Chemical Engineering, September 2, 1974.
2. J. Happel, "Chemical Process Economics," John Wiley \& Sons, Hoboken, NJ, 1958.
3. F. Holland, F. Watson, and J. Wilkinson, (adapted from) "Financing Principles of Accounting," Chemical Engineering, July 8, 1974.
4. J. Reynolds, R. Dupont, and L. Theodore, "Hazardous Waste Incineration Calculations: Problems and Software," John Wiley \& Sons, Hoboken, NJ, 1991.
5. R. Dupont, L. Theodore, and J. Reynolds, "Accident and Emergency Management: Problems and Solutions," VCH Publishers, New York, NY, 1991.
6. L. Theodore, R. Dupont, and J. Reynolds, "Pollution Prevention: Problems and Solutions," Gordon and Breach Publishers, Amsterdam, Holland, 1994.
7. K. Ganeson, L. Theodore, and J. Reynolds, "Air Toxics: Problems and Solutions," Gordon and Breach Publishers, Amsterdam, Holland, 1996.
8. R. Dupont, T. Baxter, and L. Theodore, "Environmental Management: Problems and Solutions," CRC Press, Boca Raton, FL, 1998.
9. L. Theodore and K. Neuser, "Engineering Economics and Finance," a Theodore Tutorial, Theodore Tutorials, East Williston, NY, 1996.
10. J. Reynolds, J. Jeris, and L. Theodore, "Handbook of Chemical and Environmental Engineering Calculations," John Wiley \& Sons, Hoboken, NJ, 2002.

NOTE: Additional problems are available for all readers at www.wiley.com. Follow links for this title.

